

## Purpose of study

Mathematics is a creative and highly inter-connected discipline that has been developed over centuries, providing the solution to some of history's most intriguing problems. It is essential to everyday life, critical to science, technology and engineering, and necessary for financial literacy and most forms of employment. A high-quality mathematics education therefore provides a foundation for understanding the world, the ability to reason mathematically, an appreciation of the beauty and power of mathematics, and a sense of enjoyment and curiosity about the subject.

## Aims

The national curriculum for mathematics aims to ensure that all pupils:

- become fluent in the fundamentals of mathematics, including through varied and frequent practice with increasingly comple problems over time, so that pupils develop conceptual understanding and the ability to recall and apply knowledge rapidly and accurately.
- reason mathematically by following a line of enquiry, conjecturing relationships and generalisations, and developing an argument, justification or proof using mathematical language
- can solve problems by applying their mathematics to a variety of routine and non-routine problems with increasing sophistication, including breaking down problems into a series of simpler steps and persevering in seeking solutions.

Mathematics is an interconnected subject in which pupils need to be able to move fluently between representations of mathematical ideas. The programmes of study are, by necessity, organised into apparently distinct domains, but pupils should make rich connections across mathematical ideas to develop fluency, mathematical reasoning and competence in solving increasingly sophisticated problems. They should also apply their mathematical knowledge to science and other subjects.

The expectation is that the majority of pupils will move through the programmes of study at broadly the same pace. However, The expectation is that the majority of pupils will move through the programmes of study at broadly the same pace. However,
decisions about when to progress should always be based on the security of pupils' understanding and their readiness to progress to the ext stage Pupils who grasp concepts rapidly should be challenged through being offered rich and sophisticated problem before any acceleration through new content. Those who are not sufficiently fluent with earlier material should consolidate their understanding, including through additional practice, before moving on.

Information and communication technology (ICT)
Calculators should not be used as a substitute for good written and mental arithmetic. They should therefore only be introduced near the end of key stage 2 to support pupils' conceptual understanding and exploration of more complex number problems, if written and mental arithmetic are secure. In both primary and secondary schools, teachers should use their judgement about when ICT tools should be used.

## Spoken language

The national curriculum for mathematics reflects the importance of spoken language in pupils' development across the whole curriculum cognitively, socially and linguistically. The quality and variety of language that pupils hear and speak are key factors in developing their mathematical vocabulary and presenting a mathematical justification, argument or proof. They must be assisted in making their thinking clear to themselves as well as others and teachers should ensure that pupils build secure foundations by using discussion to probe and remedy their misconceptions.

## Key Stage 1 Mathematics (Years 1 \& 2)

The principal focus of mathematics teaching in key stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value. This should involve working with numerals, words and the four operations, including with practical resources [for example, concrete objects and measuring tools].

At this stage, pupils should develop their ability to recognise, describe, draw, compare and sort different shapes and use the related vocabulary. Teaching should also involve using a range of measures to describe and compare different quantities such as length, mass, capacity/volume, time and money.

By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value. An emphasis on practice at this early stage will aid fluency

Pupils should read and spell mathematical vocabulary, at a level consistent with their increasing word reading and spelling knowledge at key stage 1 .

## Year 2 - Overview

## Number, place value \& algebra

Using materials and a range of representations, pupils practise counting, reading, writing and comparing numbers to at least 100 and solving a variety of related problems to develop fluency. They count in multiples of three to support their later understanding of a third.

As they become more confident with numbers up to 100, pupils are introduced to larger numbers to develop further their recognition of patterns within the number system and represent them in different ways, including spatial representations.
Pupils should partition numbers in different ways (for example, $23=20+3$ and
$23=10+13$ ) to support subtraction. They become fluent and apply their knowledge of numbers to reason with, discuss and solve problems that emphasise the value of each digit in two-digit numbers. They begin to understand zero as a place holder

## Calculation

Pupils extend their understanding of the language of addition and subtraction to include sum and difference.
Pupils practise addition and subtraction to 20 to become increasingly fluent in deriving facts such as using $3+7=10$; 10-7 $=3$ and $7=$ $10-3$ to calculate
$30+70=100 ; 100-70=30$ and $70=100-30$. They check their calculations, including by adding to check subtraction and adding numbers in a different order to check addition (for example, $5+2+1=1+5+2=1+2+5$ ). This establishes commutativity and associativity of addition.

Recording addition and subtraction in columns supports place value and prepares for formal written methods with larger numbers
Pupils use a variety of language to describe multiplication and division
Pupils are introduced to the multiplication tables. They practise to become fluent in the 2,5 and 10 multiplication tables and connect them to each other. They connect the 10 multiplication table to place value, and the 5 multiplication table to the divisions on the clock face. They begin to use other multiplication tables and recall multiplication facts, including using related division facts to perform written and mental calculations.
Pupils work with a range of materials and contexts in which multiplication and division relate to grouping and sharing discrete and continuous quantities, to arrays and to repeated addition. They begin to relate these to fractions and measures (for example $40 \div 2=20$, 20 is a half of 40 ). They use commutativity and inverse relations to develop multiplicative reasoning (for example, $4 \times 5=20$ and $20 \div 5=$ 4).

## Fractions, Decimals \& Percentages

Pupils use fractions as 'fractions of discrete and continuous quantities by solving problems using shapes, objects and quantities. The connect unit fractions to equal sharing and grouping, to numbers when they can be calculated, and to measures, finding fractions of
lengths, quantities, sets of objects or shapes. They meet $\frac{3}{4}$ as the first example of a non-unit fraction.

Pupils should count in fractions up to 10 , starting from any number and using the $\frac{1}{2}$ and $\frac{2}{4}$ equivalence on the number line (for example, $1 \frac{1}{4}, 1 \frac{2}{4}$ (or $1 \frac{1}{2}$ ), $1 \frac{3}{4}, 2$ ). This reinforces the concept of fractions as numbers and that they can add up to more than one.

## Measurement

Pupils use standard units of measurement with increasing accuracy, using their knowledge of the number system. They use the appropriate language and record using standard abbreviations.

Comparing measures includes simple multiples such as 'half as high'; 'twice as wide'.
They become fluent in telling the time on analogue clocks and recording it.
Pupils become fluent in counting and recognising coins. They read and say amounts of money confidently and use the symbols $£$ and $p$ accurately, recording pounds and pence separately

## Geometry - Properties of Shape

Pupils handle and name a wide variety of common 2-D and 3-D shapes including: quadrilaterals and polygons, and cuboids, prisms and cones, and identify the properties of each shape (for example, number of sides, number of faces). Pupils identify, compare and sort shapes on the basis of their properties and use vocabulary precisely, such as sides, edges, vertices and faces

Pupils read and write names for shapes that are appropriate for their word reading and spelling.
Pupils draw lines and shapes using a straight edge.
Geometry - Position and Direction
Pupils should work with patterns of shapes, including those in different orientations.
Pupils use the concept and language of angles to describe 'turn' by applying rotations, including in practical contexts (for example, pupils themselves moving in turns, giving instructions to other pupils to do so, and programming robots using instructions given in right angles)

## Statistics

Pupils record, interpret, collate, organise and compare information (for example, using many-to-one correspondence in pictograms with simple ratios $2,5,10$ ).

## Addition and subtraction

## Pupils should be taught to:

Pupils should be taught to:

- count in steps of 2,3 , and 5 from 0 , and in tens from any number, forward and backward
- recognise the place value of each digit in a two-digit number (tens, ones)
- identify, represent and estimate numbers using different representations, including the number line
- compare and order numbers from 0 up to 100 ; use < , > and = signs
- read and write numbers to at least 100 in numerals
- read and write numbers to at least 100 in words
- use place value and number facts to solve problems.
- using concrete objects and pictorial representations, including those involving numbers, quantities and measures
- applying their increasing knowledge of mental and written methods
- recall and use addition and subtraction facts to 20 fluently
- derive and use related facts up to 100
- add and subtract numbers using concrete objects, pictorial representations, and mentally, including:
- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers
- adding three one-digit numbers
- show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot
- recognise and use the inverse relationship between addition and subbraction and use this to check calculations and solve missing number problems.


## Multiplication and division

Pupils should be taught to

- recall and use multiplication and division facts for the 2,5 and 10 multiplication tables including recognising odd and even numbers
- calculate mathematical statements for multiplication and division within the calculate mathematical statements for multiplication and division within the
multiplication tables and write them using the multiplication $(x)$. division $(:)$ and multiplication tab
equals (=) signs
- show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot
- solve problems involving multiplication and division, using materials, arrays, repeate addition, mental methods, and multiplication and division facts, including problems in contexts.

Statistics

Pupils should be taught to.
interpret and construct simple pictograms, tally charts, block diagrams and simple tables

- ask and answer simple questions by counting the number of objects in each category and sorting the categories by quantity
- ask and answer questions about totalling and comparing categorical data.


## Geometry

Pupils should be taught to:
Pupils should identify and describe the properties of 2-D shapes, including the number of sides and identity and describe the prope
line symmetry in a vertical line

- identify and describe the properties of 3-D shapes, including the number of edges, identify and describe
vertices and faces
identify 2-D shapes on the surface of 3-D shapes [for example, a circle on a cylinder and a triangle on a pyramid]
compare and sort common 2-D and 3-D shapes and everyday objects.


## Pupils should be taught to

order and arrange combinations of mathematical objects in patterns and sequences

- use mathematical vocabulary to describe position, direction and movement, including movement in a straight line and distinguishing between rotation as a turn and in term

